

STRAIGHT LINES

- Distance between the points $P(x_1, y_1)$ and $Q(x_2, y_2)$ is
$$PQ = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
- Coordinates of a point dividing the line segment joining the points (x_1, y_1) and (x_2, y_2) internally in the ratio $m:n$ are
$$\left[\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right]$$
- In particular, If $m=n$, the coordinates of the mid point of the line segment joining the points (x_1, y_1) and (x_2, y_2) are
$$\left[\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right]$$
- Area of triangle vertices are $(x_1, y_1), (x_2, y_2)$ and (x_3, y_3)

$$\frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

 **Note:** If the area of the triangle ABC is zero, then three points A, B and C lie on a line, i.e., they are collinear.

Slope of a line $m = \tan\theta$ ($\theta \neq 90^\circ$)

 **Note:** The slope of x-axis is zero and slope of y-axis is not defined.

Slope of the line through the points (x_1, y_1) and (x_2, y_2)

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

If the line l_1 is parallel to l_2

$$m_1 = m_2$$

$$\tan\alpha = \tan\beta$$

If the line l_1 and l_2 are perpendicular

$$m_2 = -\frac{1}{m_1} \quad \text{OR} \quad m_1 m_2 = -1$$

$$\begin{aligned} \tan\beta &= \tan(\alpha + 90^\circ) \\ &= -\cot\alpha = -\frac{1}{\tan\alpha} \end{aligned}$$

Acute angle θ between two lines with slopes m_1 and m_2

$$\tan\theta = \left| \frac{m_2 - m_1}{1 + m_1 m_2} \right|, \quad 1 + m_1 m_2 \neq 0$$

Collinearity of three points Three points are collinear if and only if

$$\text{slope of } AB = \text{slope of } BC$$

Point-slope form

$$y - y_1 = m(x - x_1)$$

Two-point form

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1} (x - x_1)$$

Slope-intercept form

Case I $y = mx + c$

slope m and y -intercept c

Case II

$$y = m(x - d)$$

slope m and x -intercept d

Intercept form

$$\frac{x}{a} + \frac{y}{b} = 1$$

x -intercept a and y -intercept b

Normal form

$$x \cos\omega + y \sin\omega = p$$

Normal distance from the origin.

Distance of a point from a line

$$d = \frac{|Ax_1 + By_1 + C|}{\sqrt{A^2 + B^2}}$$

$Ax + By + C = 0$ from a point (x_1, y_1)

Distance between two parallel lines

$$d = \frac{|C_1 - C_2|}{\sqrt{A^2 + B^2}}$$

two parallel lines $Ax + By + C_1 = 0$ and $Ax + By + C_2 = 0$

